Balanced Dynamics and Convection in the Tropical Atmosphere¹

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How Do We Separate "Convection" from "Large Scale"? (Ooyama, 1982)

- Total atmospheric flow = balanced part + unbalanced part.
- Convection included in unbalanced part and is tightly coupled to it. This part of the flow is chaotic and unpredictable in detail.
- Balanced flow is much simpler and much more predictable.
- Only that aspect of convection controlled by the balanced part of the flow is predictable.

Adjustment to Balance by Inertia-Gravity Waves

Plane wave

amplitude
$$\propto \exp[i(kx+mz-\omega t)]$$

Dispersion relation

$$\omega^2 = f_{eff}^2 + rac{k^2 N^2}{m^2} \Rightarrow \omega^2 \ge f_{eff}^2$$

Balance time scale $< 1/{\rm Coriolis}$ parameter. At 10 N $f^{-1} \approx 10$ hr. Effective Coriolis parameter

$$f_{eff} = \zeta_a = absolute vorticity$$

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Time Scales of Convection

- \blacktriangleright Convective cell overturning time $\approx 1~{\rm hr}$
- Mesoscale convective system 2-20 hr
- Ensembles of tropical convection (easterly waves, cyclones) > 1 day

Convective time scale = time scale for changing vorticity \approx 1/mean divergence (area-dependent)

Convective time scale > adjustment time scale \Rightarrow balance

Regime Diagram (Inspired by Ooyama)



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log(absolute vorticity)

Thermodynamic Control of Convection

From Raymond and Sessions (2007); Sessions et al. (2015); in weak temperature gradient models, rain increases as:

- surface moist entropy flux increases;
- saturation fraction (a measure of column relative humidity) increases;
- instability index (a measure of lower to upper-tropospheric moist convective instability) decreases (within limits).

Instability index decreases as mid-level vorticity increases.

Instability Index = saturated moist entropy 1-3 km minus saturated moist entropy 5-7 km



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Instability Index and Convection



mass flux

large instability index strong entropy detrainment

small instability index weak entropy detrainment

Hagupit 2 – Non-Developing Wave



Instability index = 27 J/K/kg

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Nuri 2 – Rapidly Developing Cyclone



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Nuri 2

Instability index = 11 J/K/kg

Potential Vorticity and Temperature Perturbations (Balanced State)



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Nuri1 and Nuri2 PV Inversions



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Vorticity and Convection

- Mid-level vorticity produces a temperature dipole with a warm anomaly aloft and a cool anomaly at low levels.
- This temperature dipole results in lower instability index.
- Lower instability index produces bottom-heavy convective mass fluxes, which increases precipitation and aids in tropical cyclone spinup.

It also results in weaker moist entropy detrainment or even entropy entrainment.

Instability Index and Mid-Level Absolute Vorticity (TPARC/TCS08 and PREDICT)



SAC

Can We Predict Rainfall? Measure of Strength of Convection

- Recipe: Linear combination of...
 - Surface moist entropy flux (eflux)
 - 500 hPa vorticity (surrogate for instability index; vort500)
 - Saturation fraction (column relative humidity; satfrac)
- ▶ Inspired by Raymond and Flores (2016).

rain = A + B*eflux + C*vort500 (+ D*satfrac)

Predicted vs. Actual Rainfall (with humidity)



rain_p = -64 + 16.3*eflux + 269*vort500 + 73*satfrac

Predicted vs. Actual Rainfall (no humidity)



actual rain (mm/d)

rain_p = -13.2 + 18.0*eflux + 350*vort500

Moisture Quasi-Equilibrium



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How Does MQE Work? (Singh and O'Gorman, 2013)



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Summary of Forcing of Tropical Oceanic Rainfall

- Three controlling variables
 - Surface moist entropy flux
 - Strength of mid-level vorticity (instability index)

- Saturation fraction
- However: Saturation fraction is slaved to mid-level vorticity as long as convection is strong and environmental ventilation is weak.

TCS08-PREDICT Regime Diagram (300 km scale)



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Examples from DYNAMO



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Dynamo Regime Diagram (500-1000 km scale)



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Moisture Quasi-Equilibrium in DYNAMO



Instability Index vs. Mid-Level Relative Vorticity



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Entropy Budget and Intensification of Tropical Cyclones

- Case studies of tropical cyclones in various phases from HS-3, PREDICT/IFEX, and TCS-08
- Arrays of dropsondes and satellite data used to compute entropy budget
- Storm intensification correlated with positive column entropy tendency
- This test could be done operationally with G-V dropsonde arrays around TCs

Entropy Tendency and TC Intensification (Ana Juračić)



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Interaction of Convection and Balanced Disturbances



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